

Logistic Equation Warm-Up

Introduction to Epidemiological Modeling

College of the Atlantic. April 7, 2023

Consider again the differential equation

$$\frac{dP}{dt} = f(P), \quad (1)$$

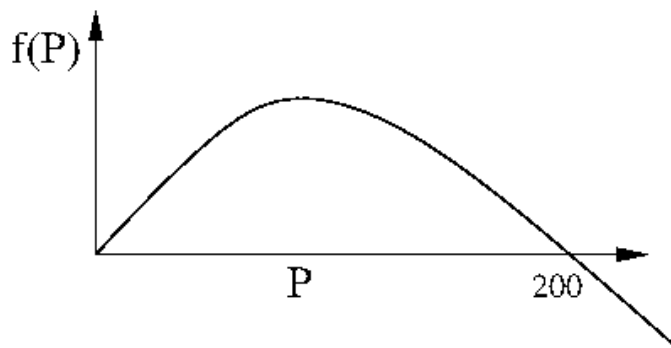
where $f(P)$ is shown in the figure. We will only consider non-negative P .

1. Sketch a few representative¹² solutions $P(t)$ to Eq. (1).
2. A possible formula the $f(P)$ in Eq. (1) is:

$$f(P) = kP\left(1 - \frac{P}{K}\right), \quad (2)$$

where K and k are positive constants.

- (a) Convince yourself that the graph of Eq. (2) looks like the figure.
 - (b) What is the practical meaning of K ? If K is doubled, how do the solutions $P(t)$ change?
 - (c) What is the practical meaning of k ? If k is doubled, how do the solutions $P(t)$ change?
3. To what situation(s) might Eq. (1) apply?



¹I.e., choose a few different initial conditions that, taken together, give an overview of the sorts of things solutions to the equation can do.

²This is the same thing we did in class on Tuesday.