Chapter C4: Particles and Systems

C4.1: Systems of Particles

- 1. Particles are tiny.
- 2. A system is a collection of particles with a boundary.
- 3. Internal interactions are interactions between particles or objects in a systems.

C4.2: Conservation of Momentum

- 1. The total momentum of a system is just the sum of the momenta of the objects in the system. This is Eq. (C4.1).
- 2. If a system experiences no external interactions, then its total momentum is conserved; \vec{p}_{tot} does not change.

C4.3 Center of Mass

- 1. Eq. (C4.2), Eq. (C4.3) and Eqs. (C4.4a–c) are identical. They are different ways of writing the same thing.
- 2. The equation that defines the center of mass is the equation for a *weighted average*.

average test score
$$= \frac{1}{N} (s_1 + s_2 + \cdots + s_N)$$

average test score weighted by height = $\frac{1}{h_1 + h_2 + \cdots + h_N} (h_1 s_1 + h_2 s_2 + \cdots + h_N s_N)$.

C4.4: How the Center of Mass Moves

- 1. A system's momentum can be found via the velocity of its center of mass: $\vec{p}_{tot} = M \vec{v}_{CM}$. This is Eq. (C4.14).
- 2. "A system's center of mass responds to its external interactions exactly as a point particle would respond to those interactions." (p. 71)

C4.5: Inertial Reference Frames

The main point here is that we should choose our reference frames such that they're non-accelerating. If some of the technical details seem a little strange, don't worry.

C4.6: Interactions with the Earth

The earth is way bigger than you.

Center of Mass Practice

- 1. A 20 kg and a 60 kg object are 2 m apart. What is the center of mass of the two-object system?
- 2. Determine the center of mass of the system shown in Fig. (1). Express your answer in both coordinate and magnitude-direction form.



Figure 1: